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Handling Missing Data: The Motivation and Method of Multiple Imputation

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Introduction

• Missing data a problem in nearly all studies

• Standard methods for handling missing data generally not appropriate

• Multiple imputation a principled (and fairly straightforward) way to handle missing data

This symposium will...

• Provide an overview of missing data and multiple imputation

• Give guidance on how to create and use multiply imputed data using easy-to-use software

• Show an illustration of the use of multiply imputed data

Motivating example: CMHI National Evaluation

• National evaluation of CMHS Children and Their Families Program (CMHI)

• Longitudinal data

• 9,185 children

• In 45 sites that received funding from 1997-2000

• 396 variables at baseline! (demographics, behavior, substance use, delinquency)

Rates of missingness in CMHI data

Variable	% Missing
Date of birth	1.7
Sex	1.7
Race	10.8
Family income	11.9
DSM-IV diagnoses	23.8
% of day in special ed	40.0

Types of missing data

- "Missing completely at random" (MCAR)
  - Probability of variable being missing does not depend on anything
- "Missing at random" (MAR)
  - Probability of variable being missing depends on observed variables
- "Not missing at random" (NMAR)
  - Probability of variable being missing depends on observed and unobserved variables (e.g., the value that is missing)

What can we do?

- MCAR:
  - Complete case analysis okay
- MAR:
  - Need to use observed values to help predict ("impute") what missing values are
- NMAR:
  - Requires a more complex model for missing data process

Standard Approaches

- Complete case analysis
  - Assumes MCAR: generally unreasonable
  - Often results in substantial loss of power
- Single imputation approaches (hot deck, mean imputation, regression prediction imputation)
  - Does not incorporate uncertainty in imputation
  - Analysis treats imputed values as being the true (observed) values
  - Results will have lower variance than they should: anti-conservative

Multiple imputation (MI)

- Main idea: Impute each missing value multiple times
  - e.g., Create 5-10 "complete" data sets, each of which has missing values filled in
- Accounts for uncertainty in imputations
- Results in correct standard errors, p-values

Steps to doing MI

- Create multiple imputations
- Do standard "complete data" analysis on each imputed data set
- Combine results across data sets
  - Incorporates both "within" and "between" imputation variability
  - ** Steps 2 and 3 often done together automatically in standard software

Step 1: Creating imputations

- Use "multiple imputation by chained equations" (MICE)
- Fits model for each variable conditional on all others, generates predictions from that model
  - Uses stepwise selection to pick model
- Iterates across variables

Benefits of MICE

• Allows realistic models for each variable
  – e.g., Age modeled as continuous variable, poverty status as binary, level of symptoms as categorical
• Can incorporate constraints
  – e.g., Number of times smoked only defined for those who had smoked at least once
• Can incorporate limits
  – e.g., Age at first use

Step 2: Analyzing Each Dataset

• Standard analysis run in each of the complete data sets
  – e.g., linear regression, survival model
• Means that complex models can be run
  – (Unlike maximum likelihood based approaches, which only work for certain models)

Step 3: Combining Results

• After analysis run on each complete dataset, combine results across datasets
• Overall estimate = average across the datasets
• Variance of that estimate = average variance of each analysis + variance across analyses

How do I actually do this?

That's what we'll cover in the next talks…

Conclusions

• Important to account for missing data in any analysis
• Multiple imputation one way to do so in a principled way
• MICE one fairly easy and flexible way of implementing MI
• But of course complexities remain…

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Guidelines and Suggestions on How to Multiply Impute Missing Data

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Session Overview

- Software
- Suggested Steps in the MI process
- Points for Consideration

Where to Begin?

- Software
  - Stata
    - ICE
  - SAS
    - PROC MI
    - **IVEware**
  - R
    - MICE

Multiple Imputation Process

- Preparing to impute data
- Creating the imputation model
- Running and Checking the model
- Diagnostics

Preparing to Impute the Data

- Create a list of variables in dataset
  - Calculate % missing
  - Classify & group by type of variable
  - Note coding
  - Note variables to transfer or drop
  - Note missing by design

Create Imputation Model

- Specify variables to be imputed
  - Type of variable
- Model Specification Options
  - Restrictions
  - Bounds
  - Interactions
  - Step-wise
  - Minimum # predictors

Sample Model

DEFAULT categorical;
COUNT livmon livdays totadu susa11d;
CONTINUOUS age berist berfit;
DROP liv1bm liv1bd;
TRANSFER childid agencyid;
RESTRICT homecat(atleast5=1) susa3(susa1=1, atleast11=1)
BOUNDS age(<=22) berist(>=0, <=45)
INTERACT ref1*sex poverty*race
MAXPRED susa5(2) susa10d(3)

Points of Consideration

• Impute items or summary scores

• Time intensive
  – Start small
    • 1-2 iterations
    • A portion of the data

Running & Checking the Model

• Review output
  – Regression models

  Impute PSCYCHP
  Code: 1
  Unperturbed and perturbed coefficients
  Intercept   0.1859464267   0.1829665596
  FAMABU   -0.5899234004   -0.5839740193
  PARNTAB   -0.8399670308   -0.8154692172

Running & Checking the Model

Review output
  – Summary Statistics

Variable SRVOUTP

Code	Observed Freq	Per	Imputed Freq	Per	Combined Freq	Per
0	2435	28.53	222	34.21	2657	28.93
1	6101	71.47	427	65.79	6528	71.07
Total	8536	100.00	649	100.00	9185	100.00

Summary Statistics

Variable SUSA5A

	Observed	Imputed	Combined
Number	710	8475	9185
Minimum	0	0	0
Maximum	30	4.5036e+015	4.5036e+015
Mean	1.96197	5.31398e+011	4.90321e+011
Std Dev	4.24563	4.89204e+013	4.69916e+013

Summary Statistics

Variable HOMECAT

Code	Observed Freq	Per	Imputed Freq	Per	Combined Freq	Per
0	762	10.36	126	6.87	888	9.67
1	1258	17.11	147	8.02	1405	15.30
2	1259	17.12	475	25.91	1734	18.88
3	4073	55.40	799	43.59	4872	53.04
4	0	0.00	286	15.60	286	3.11
Total	7352	100.00	1833	100.00	9185	100.00

Diagnostics

- Graphical comparisons
  - Overlaid histograms

Graphical Example

Graphical Example

Numerical Comparisons

- Consider characteristics of data when deciding what to compare
  - Variable level
  - Site level
- Conduct multiple types of comparisons
  - Complete missingness
    - Imputations based primarily on data from other sites
  - Differences in means & variances pre-post imputation
    - Need to determine whether differences are reasonable
- Compare versions of imputed data
  - Sensitivity to imputation model used

Before Releasing Data

- Process the data
- Documentation & Support

Conclusions

- Multiply imputing data is feasible
- Spend time upfront
- Start small and work your way to your full dataset
- Examine the imputation model and run diagnostics
- Prepare your team to work with the data

How Do I Analyze Imputed Data?

Coming up next….

References & Resources

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Employing Multiple Imputation (MI) Analysis Techniques to Examine Racial Disparities in Service Use Among Children

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Overview

- Context on substantive issue
- Methods
- Analyzing MI data
  - Commands
  - Challenges
- Results
- Discussion

Race & Service Use

- Racial minorities have the greatest unmet need for mental health services [1-2]
  - African American youth less likely to use mental health services
  - More likely to suffer from untreated mental health problems [3-5]
- Untreated mental health conditions can lead to poor school performance, violence, delinquency [6-7]

Purpose of Study

- To examine the association between race and past year mental health service use
  - Utilizing multiple imputed data was important in this study given the nature of the dataset

Method

- Data Source
  - Baseline data from national evaluation of CMHI
  - 43 sites funded 1997-2000
- Study sample (n=3649)
  - Children 5-18 years (M=12.2, SD=3.24)
  - African American or Caucasian
  - Clinical diagnosis of internalizing, externalizing, ADHD, or co-occurring disorder

Method

- Variables
  - Service use
  - Socio-demographic characteristics
  - Clinical diagnosis
  - Functional impairment
- Analyses
  - Descriptive statistics
  - Random effects regression models

Description of Sample
(n =3649)

African American	31%
Male	69%
Co-morbid Diagnosis	47%
Income <$15,000	48%
Received Services	89%
Referred from MH Agency	33%

Data Analysis Steps

- Decide whether to use original data or imputed data
  - 33% of the sample was lost due to list-wise deletion
- Select Software
  - Stata 10, R, SAS, HLM, Mplus
- Prepare to analyze imputed data
  - Read "Overview of Multiple Imputation and Using Multiply Imputed Data" by Melissa Azur, Constantine Frangakis, & Liz Stuart

Preparing to Analyze Imputed Data

- Download Stata commands
  - mimstack & mim
  - miset & mifit
  - mijoin & micombine
- Combine the five multiply imputed datasets into one dataset
  - mimstack, m(5) so ("childid") nomj0 istub (impset)
- Drop variables not of interest

Analyzing Imputed Data

- Started out working with 1 dataset until comfortable with mim commands
- Needed to learn modified commands
  - For example for descriptive statistics:
    - mim: mean age vs sum age
    - mim: proportion sex vs tab sex

Lesson Learned

Calculating sample characteristics

- tab sex

male	69.44%	12,740
female	30.56%	5,608
		18,348

- mim: proportion sex

Multiple-imputation estimates	proportion	Imputations =				5
Regression estimation	Minimum obs =					3649
	Minimum dof =					398.6

	Coef.	Std. Err.	t	P>|t|	[95% Conf. Int.]	df
male	.69436	.00799	86.90	0.000	.678651 .710068	398.6
female	.30564	.00799	38.25	0.000	.289932 .321349	398.6

Analyzing Imputed Data

- Comparing differences is cumbersome (t-test, χ^2)
- For example, to compare proportions
  - **mim: proportion var1 if var2==0**
  - **mim: proportion var1 if var2==1**
  - **mim: logit var1 var2 (to obtain p-value)**

Analyzing Imputed Data

- Models were built in same way as standard analyses except commands prefaced with "mim"
  - **e.g., mim: xtlogit curserv race sex age, or i(siteid1b)**
- Traditional Likelihood Ratio Test commands do not work with mim
  - **Alternative:**
    - **Ran test on 2 individual imputed datasets & compared results**

Results
Odds Ratios & 95% Confidence Intervals

Race	Any Service	Outpatient	School	Day Tx	Inpatient/ Residential
Unadjusted					
African American	.67 (.51-.89)*	.76 (.62-.93)*	.76 (.63-.91)*	.92 (.72-1.18)	.70 (.58-.94)*
**Adjusted					
African American	.73 (.55-.98)*	.83 (.67-1.02)	.79 (.65-.95)*	1.03 (.80-1.32)	.80 (.65-.98)*

** Adjusted for sociodemographic characteristics, clinical diagnosis, functional impairment, and referral source

Discussion

- Challenges to Employing MI techniques
  - Had to understand the results in the context of multiply imputed data
  - Deciding which type of multiple imputation commands to use
  - Finding alternative commands and ways to analyze the data appropriately

Discussion

- Benefits
  - Have more complete dataset to work with
  - Building models was not complicated
  - Analyses were conducted generally in the same way as analyses with non-imputed data
- Suggestions
  - Use available resources
  - Keep a syntax (or .do) file
  - Keep output or logs of all analyses

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